

1) Let $R$ be the region bounded by the graphs of $y=\sin (\pi x)$ and $y=x^{3}-4 x$, as shown in the figure above.
a) Find the area of $R$.
b) The horizontal line $y=-2$ splits the region $R$ into two parts. Write, but do not evaluate, an integral expression for the area of the part of $R$ that is below this horizontal line.
c) The region $R$ is the base of a solid. For this solid, each cross section perpendicular to the $x$-axis is a square. Find the volume of this solid.
d) The region $R$ models the surface of a small pond. At all points in $R$ at a distance $x$ from the $y$-axis, the depth of the water is give by $h(x)=3-x$. Find the volume of water in the pond.
